



# Mastery Maths Parent Workshop

7<sup>th</sup> February 2pm  
10<sup>th</sup> February 6pm

# Mastery of Mathematics is.....

- Achievable for all
- **Deep** and sustainable learning
- The ability to build on something that has already been sufficiently mastered
- The ability to reason about a concept and make connections
- Conceptual and procedural fluency

# Teaching for Mastery

- The belief that all pupils can achieve
- Keeping the class working together so that all can access and master mathematics
- Development of **deep** mathematical understanding
- Development of both factual/procedural and conceptual fluency
- Longer time on key topics, providing time to go deeper and embed learning



# What does it mean to master something?



If you drive a car, imagine the process you went through...

- The very first drive, lacking knowledge of what to do to get moving
- The practice, gaining confidence that you are able to drive
- The driving test, fairly competent but maybe not fully confident
- A few years on, it's automatic, you don't have to think about how to change gears or use the brake
- Later still, you could teach someone else how to drive

## In the past ....



- Children who were quick graspers were being accelerated quickly through the curriculum without allowing them to secure a deep understanding of each concept.
- Children who struggled with maths were given easier tasks and did not always access the same curriculum that the quick graspers did.
- As a result children had large gaps in their mathematical understanding.

$$5 \times 4 = 20$$

factor (or multiplicand)      factor (or multiplier)      product

Addition:

$$8 + 3 = 11$$

Addend      Addend      Sum or Total

**Division Vocabulary**

dividend      divisor

$40 \div 5 = 8$

quotient



Subtraction

minuend      difference

$$57 - 34 = 23$$

operation      subtrahend

# Mathematical fluency – what is it?

$$15 \times 12 = 180$$

How could we solve this?

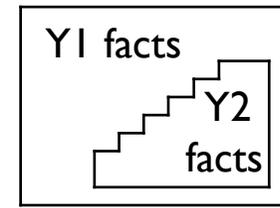
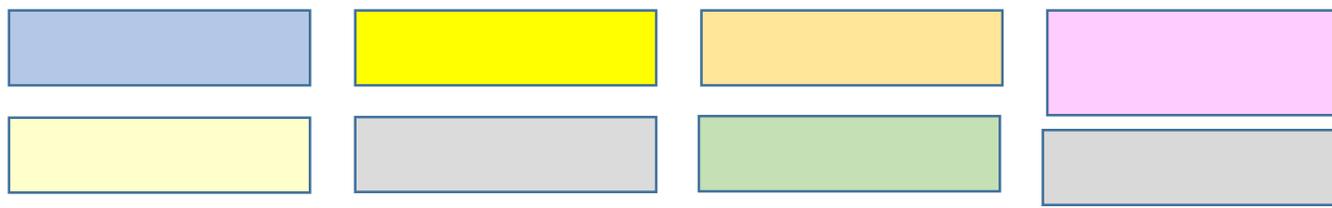
*Fluency is the ability to make connections and select the most appropriate/ efficient methods.*

# Fluency is more than memorising facts

To become fluent mathematicians, children need to develop:

- an understanding of the meaning of the operations and their relationships to each other. E.g. inverse operations.
- an understanding number relationships. E.g.  $4 \times 5$  is related to  $4 \times 50$ .
- confident use of calculating with 10, 100 and 1000. E.g.  $24 + 10 = 34$  or  $24 \times 10 = 240$ .

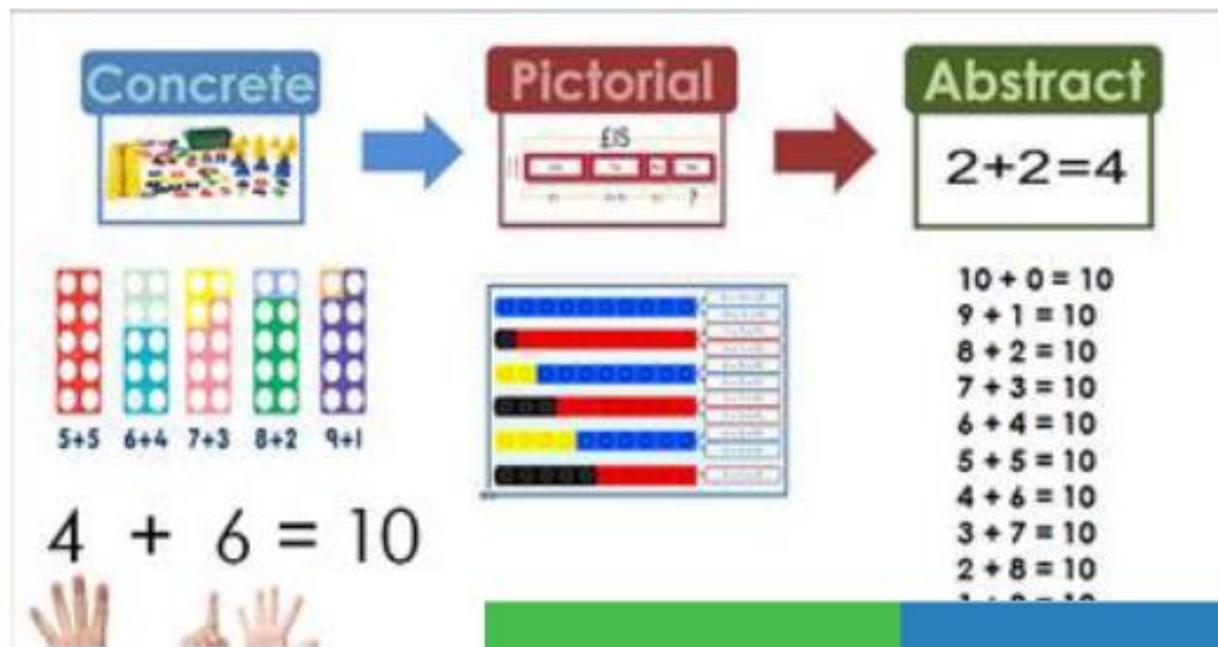
Learning number facts  
What addition facts do  
children need to know by  
the end  
of Year 2?



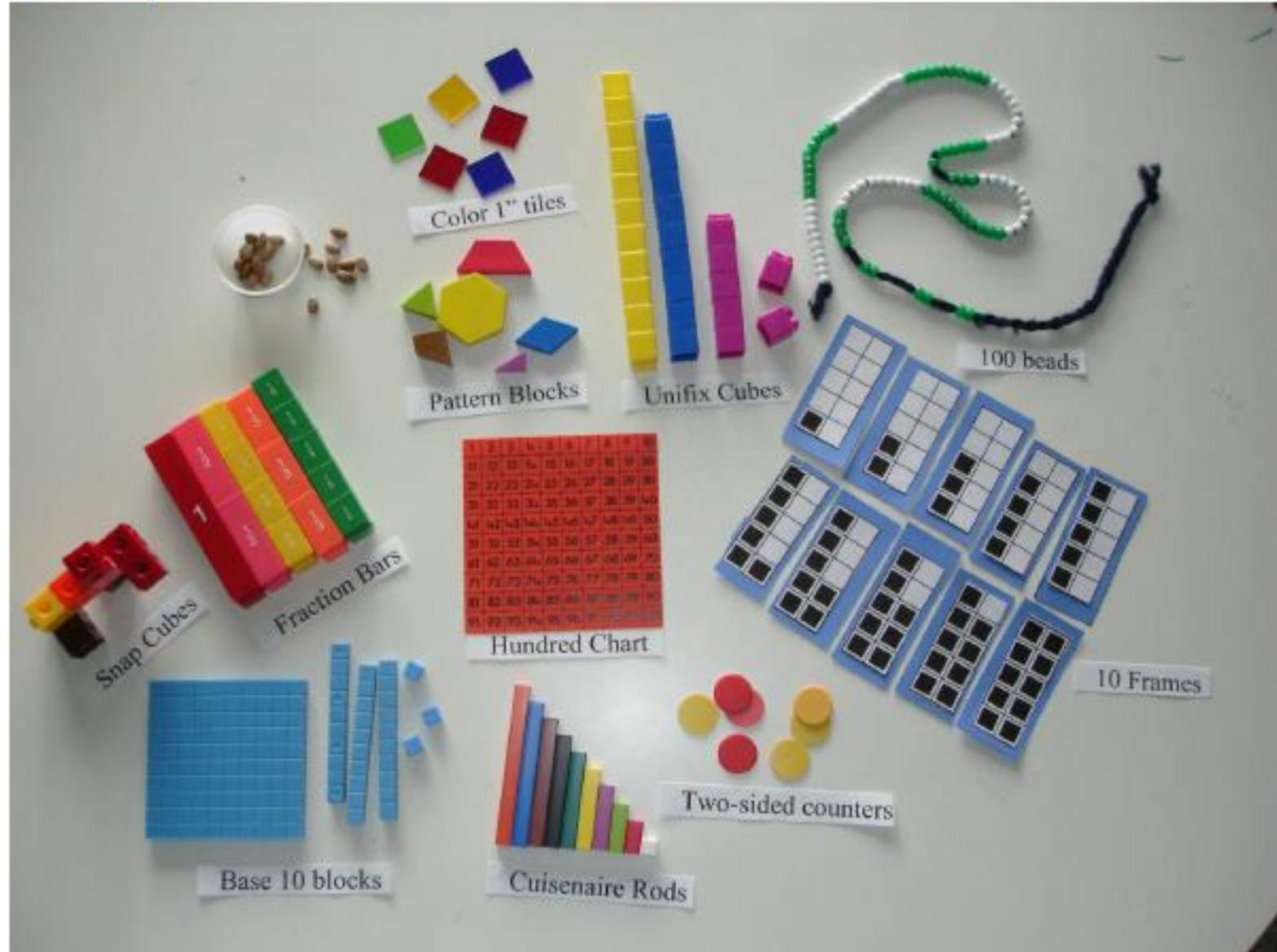
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0	0+0	0+1	0+2	0+3	0+4	0+5	0+6	0+7	0+8	0+9	0+10
1	1+0	1+1	1+2	1+3	1+4	1+5	1+6	1+7	1+8	1+9	1+10
2	2+0	2+1	2+2	2+3	2+4	2+5	2+6	2+7	2+8	2+9	2+10
3	3+0	3+1	3+2	3+3	3+4	3+5	3+6	3+7	3+8	3+9	3+10
4	4+0	4+1	4+2	4+3	4+4	4+5	4+6	4+7	4+8	4+9	4+10
5	5+0	5+1	5+2	5+3	5+4	5+5	5+6	5+7	5+8	5+9	5+10
6	6+0	6+1	6+2	6+3	6+4	6+5	6+6	6+7	6+8	6+9	6+10
7	7+0	7+1	7+2	7+3	7+4	7+5	7+6	7+7	7+8	7+9	7+10
8	8+0	8+1	8+2	8+3	8+4	8+5	8+6	8+7	8+8	8+9	8+10
9	9+0	9+1	9+2	9+3	9+4	9+5	9+6	9+7	9+8	9+9	9+10
10	10+0	10+1	10+2	10+3	10+4	10+5	10+6	10+7	10+8	10+9	10+10

Children need different to learn different methods – not just memorise these facts. They will develop an understanding of which method is the most appropriate. E.g. near doubles.

# Concrete and Pictorial Resources

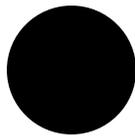
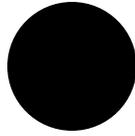
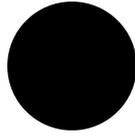


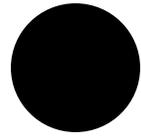
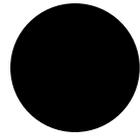
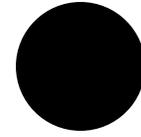
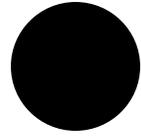
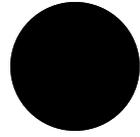
# Representation and Structure

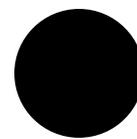
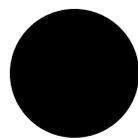
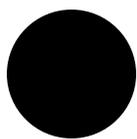
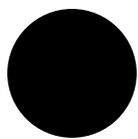
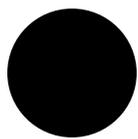


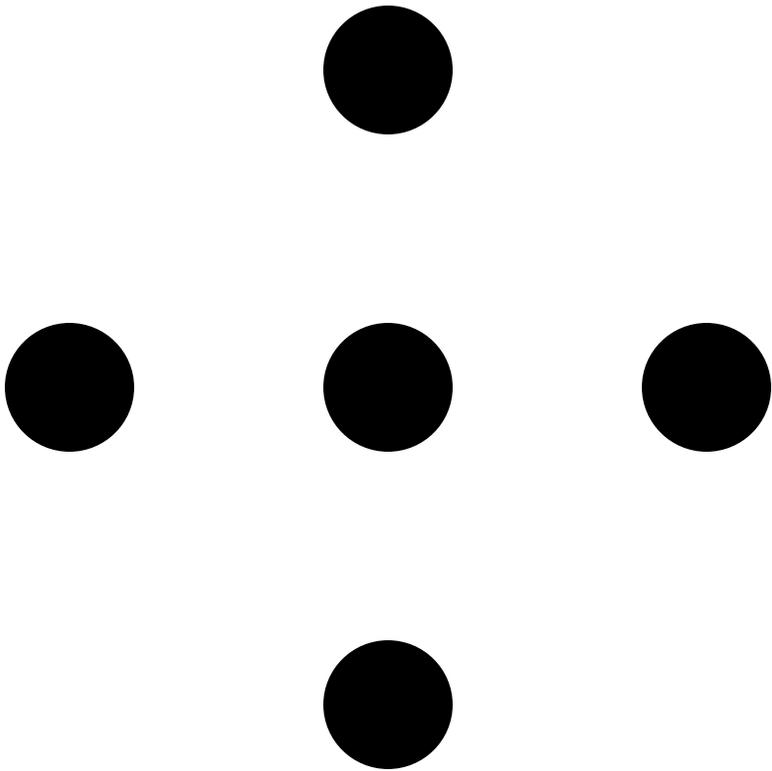
# Subitising – counting in the Early Years

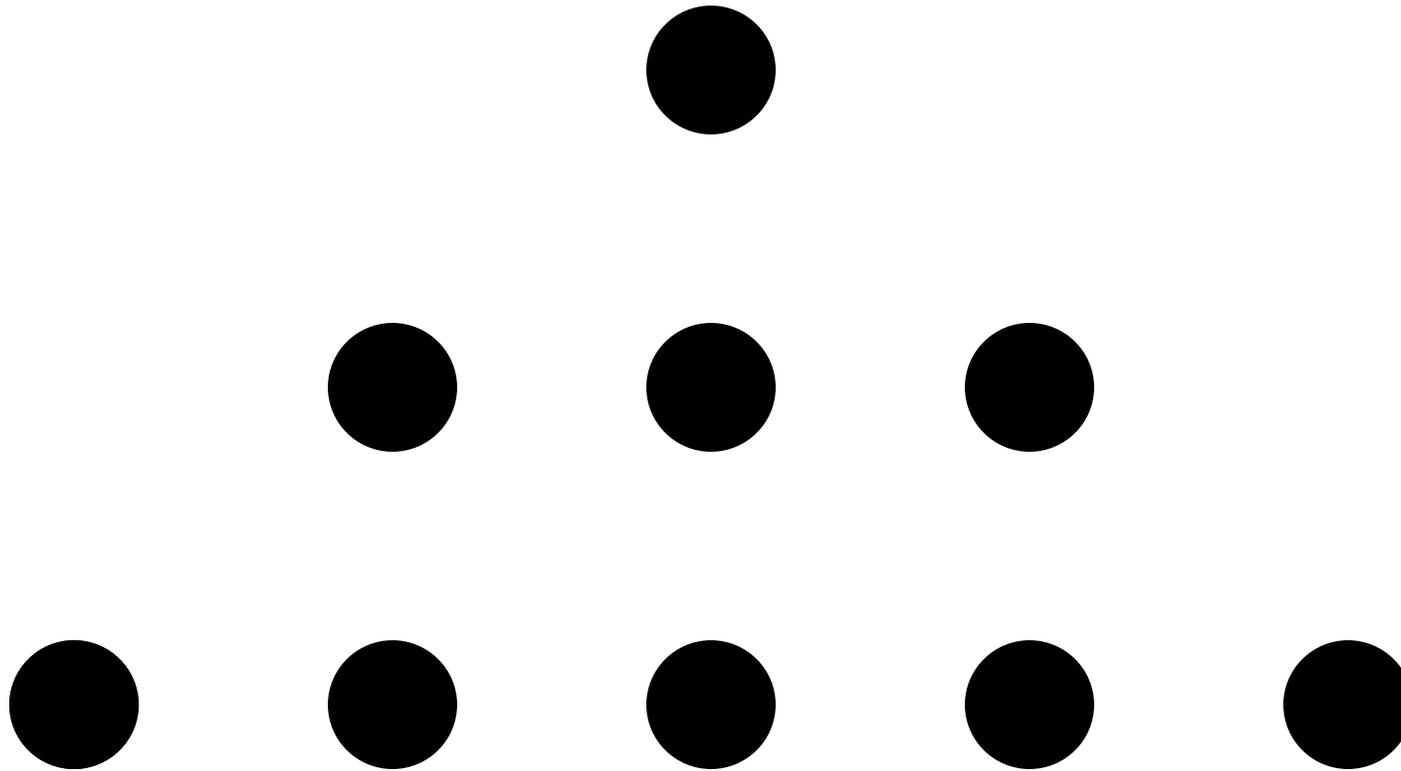
- The ability to instantly identify a set or group of objects without counting them (usually up to 6).





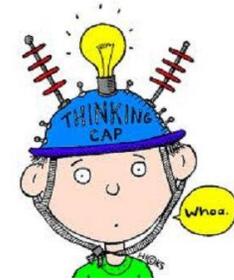
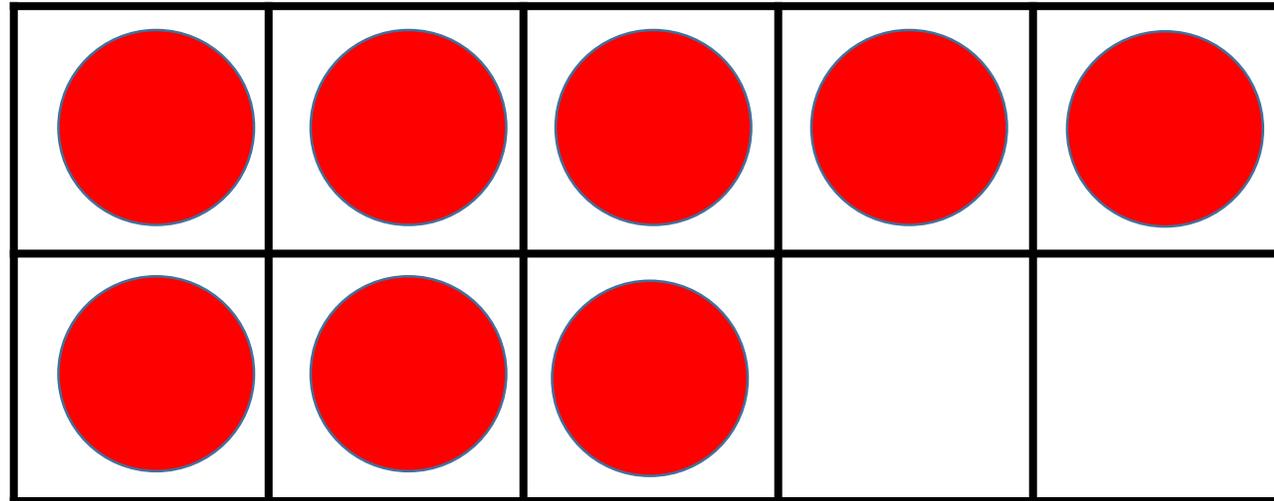


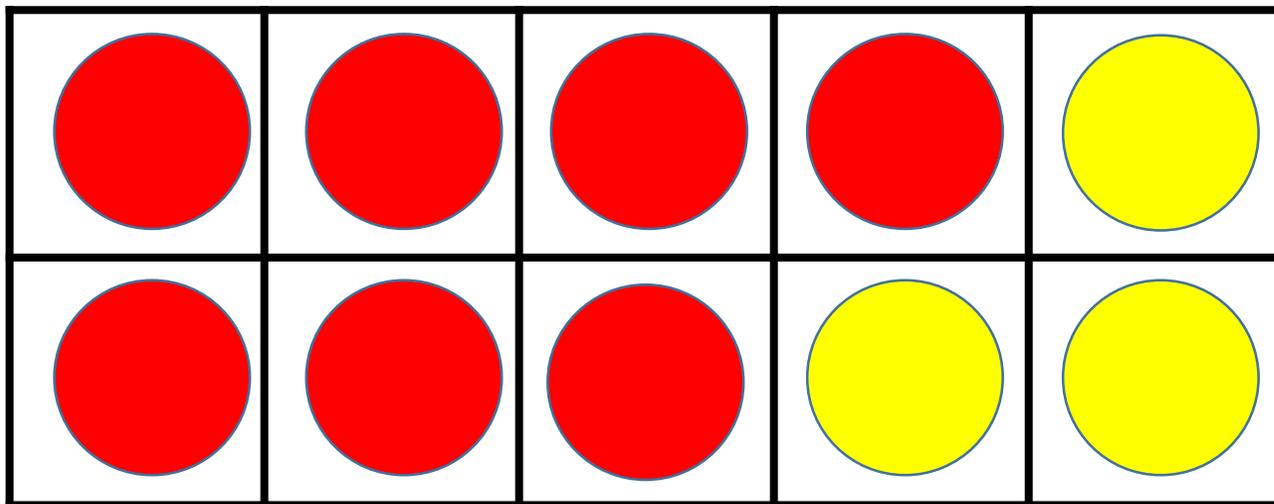




# Ten Frame used to develop number sense and fluency

What do you see?



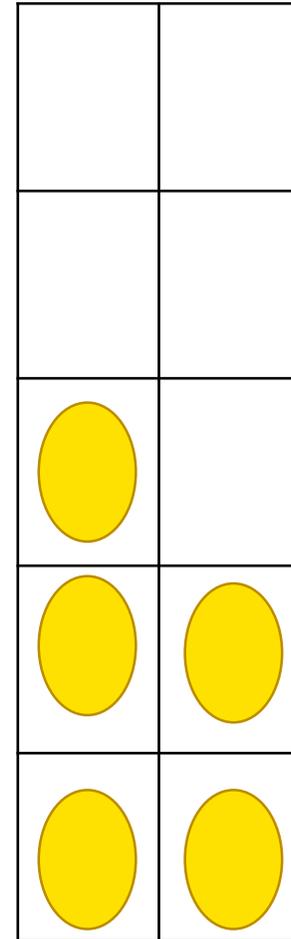
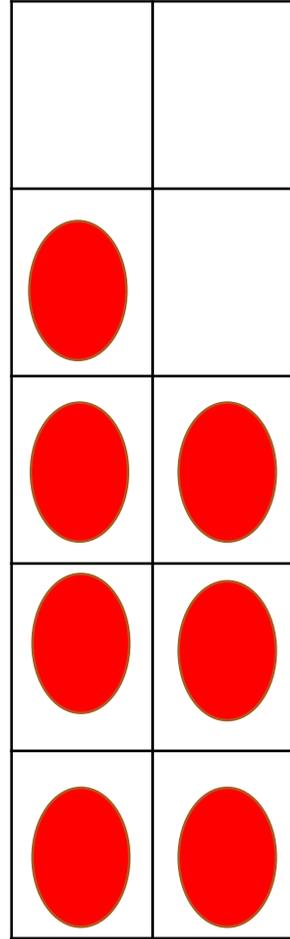


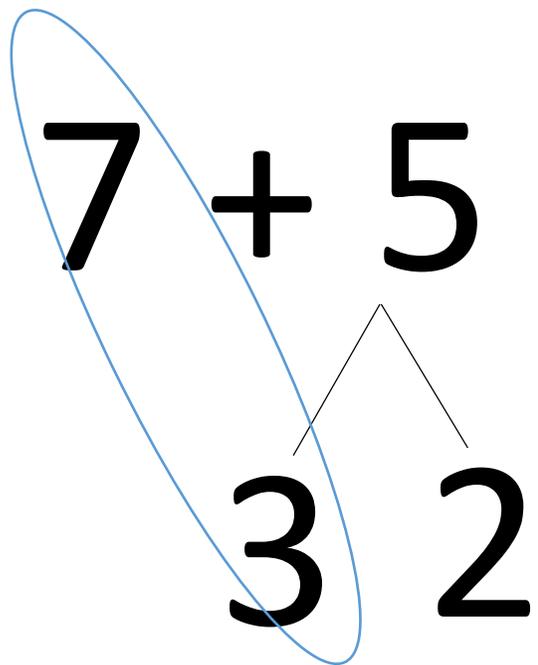
# Bridging through 10

## 'Make 10'

$$7 + 5$$

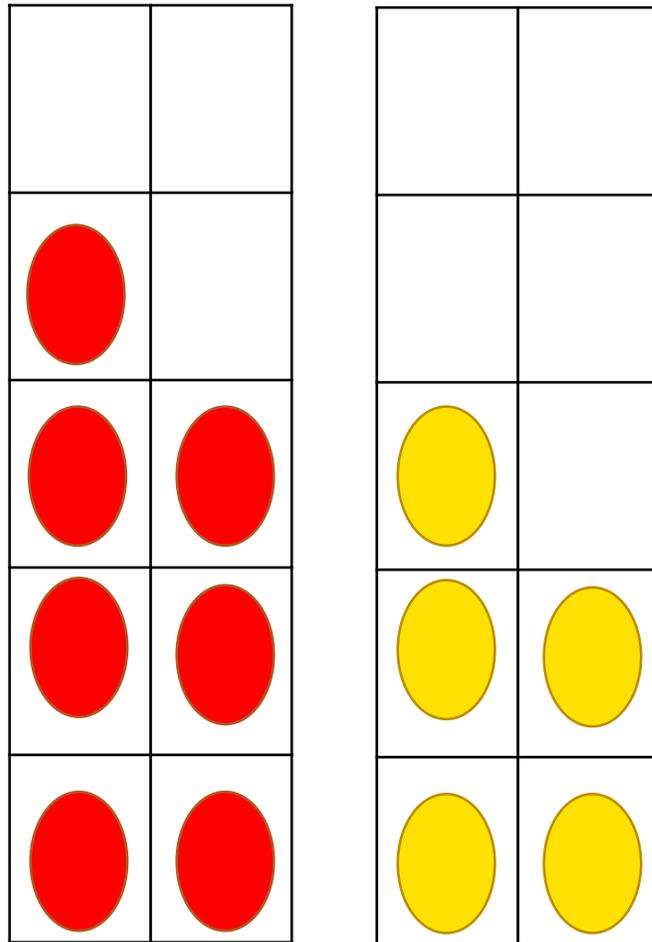

$$7 + 5$$





$$7 + 3 + 2$$

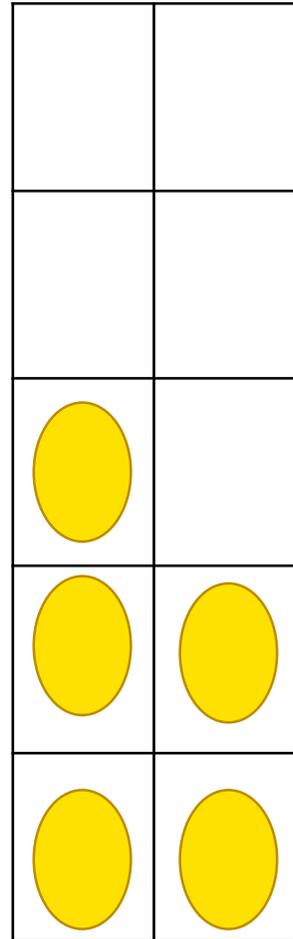
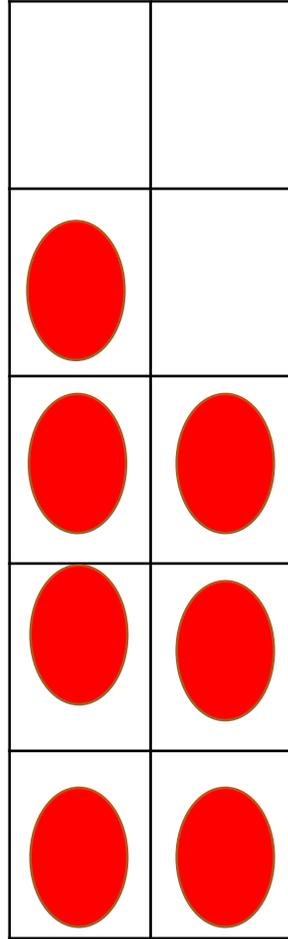
$$10 + 2$$



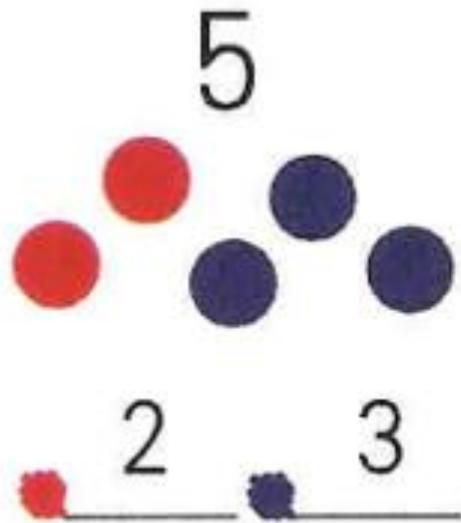
$$7 + 5$$

A diagram showing the number 7 decomposed into 2 and 5. A blue oval encircles the 5 in the second term of the equation. A thin line connects the top of the 7 to the top of the 5 in the second term, with a tick mark on the 7 side, indicating that 2 is being taken from 7 to combine with the 5.

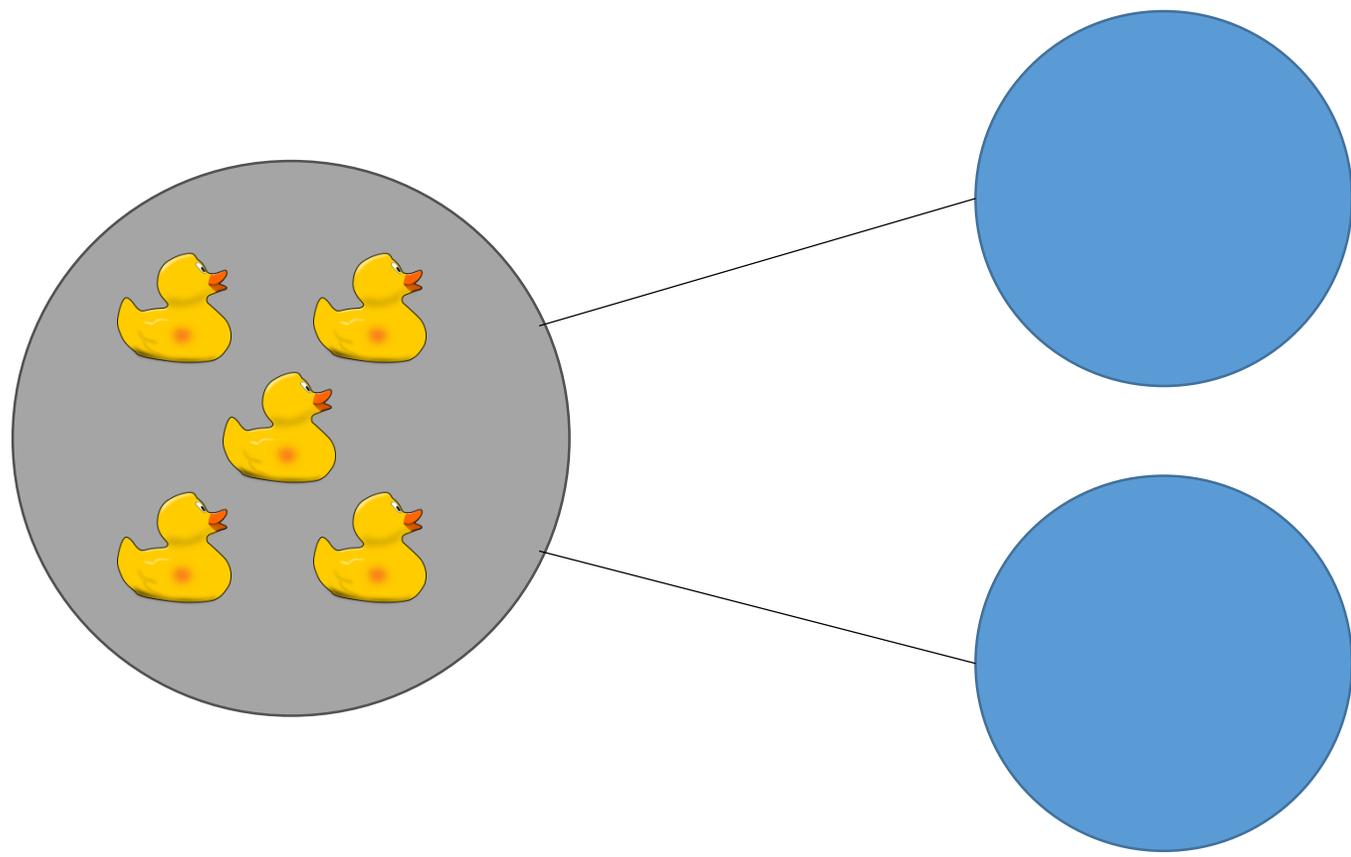
$$5 + 5 + 2$$

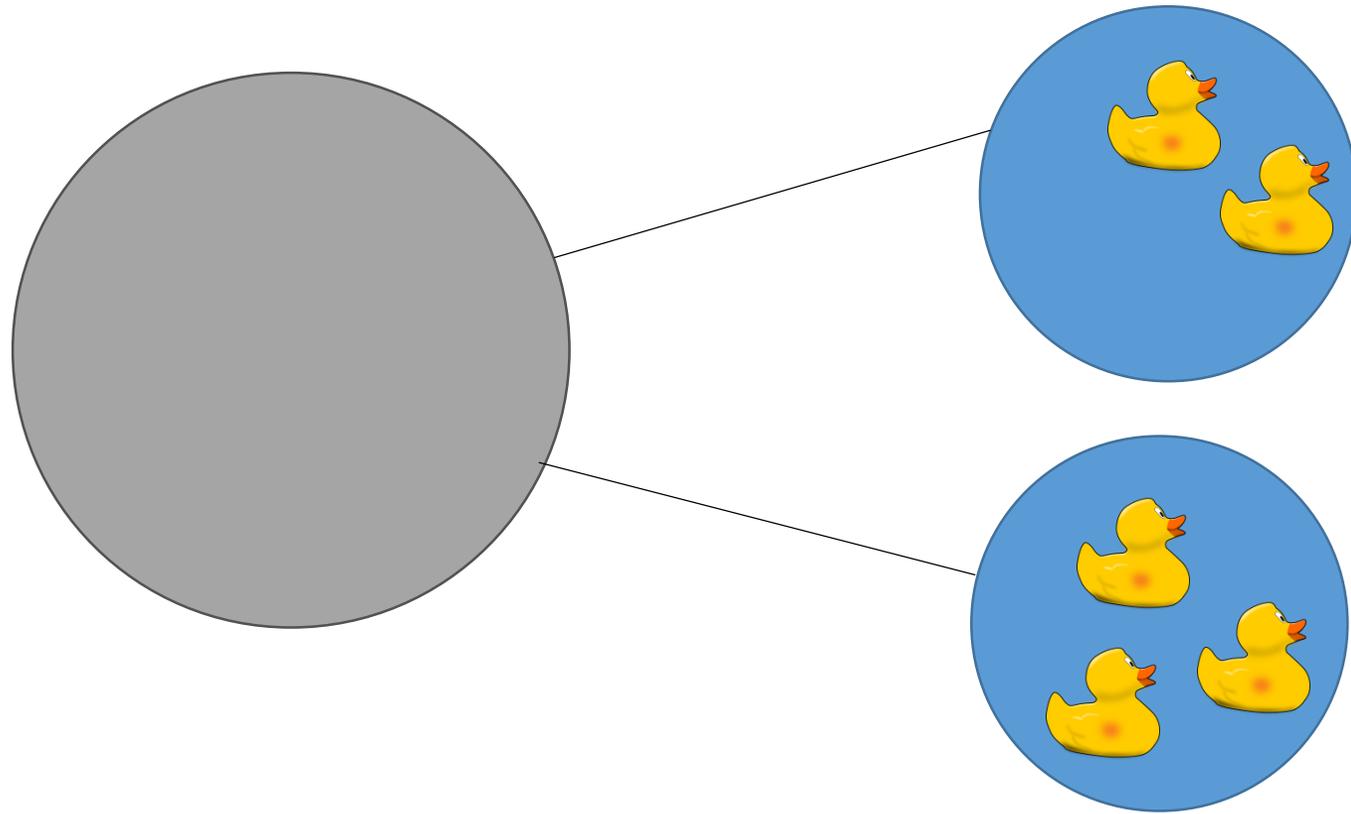


# Part – Whole Relationships

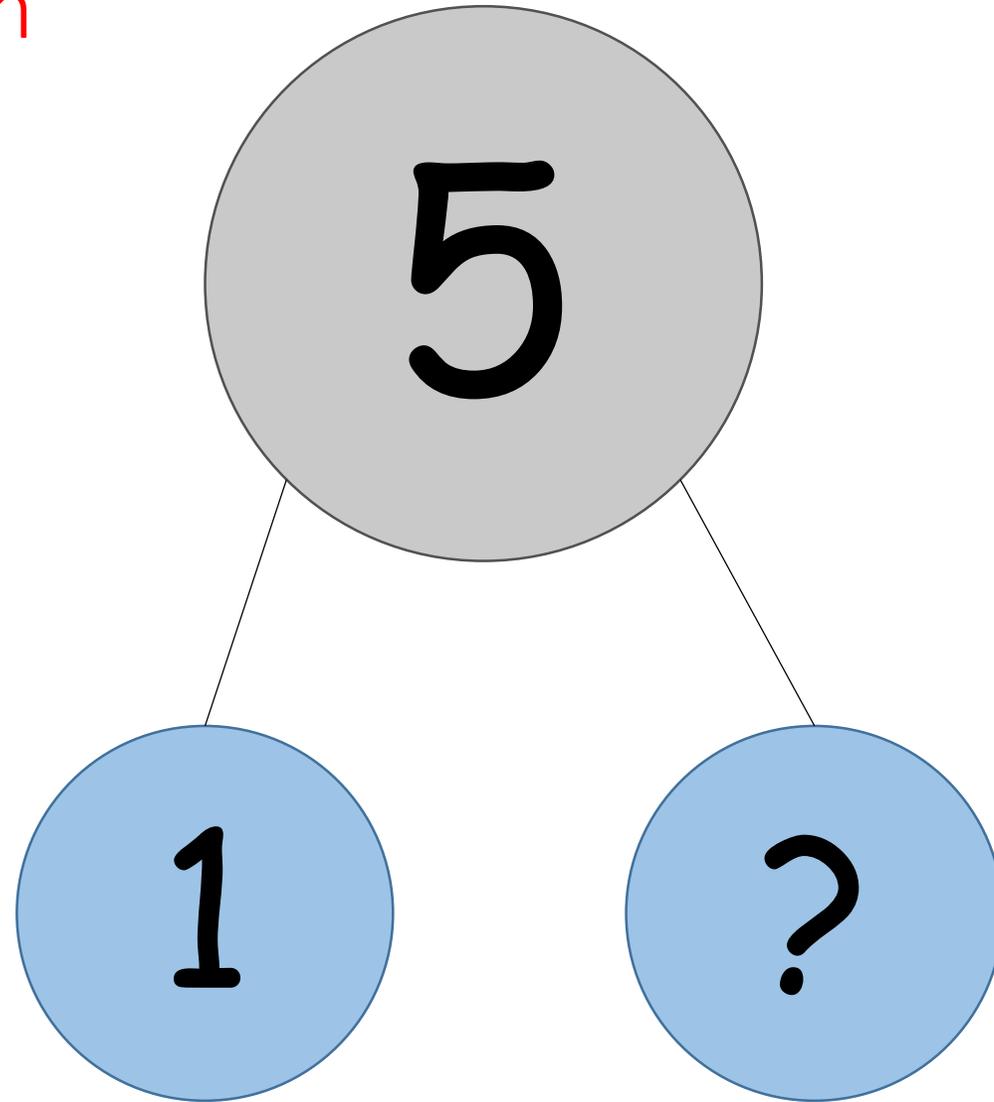


	Red	Blue
● ● ● ● ●		
● ● ● ● ●		
● ● ● ● ●	3	2
● ● ● ● ●		
● ● ● ● ●		
● ● ● ● ●		

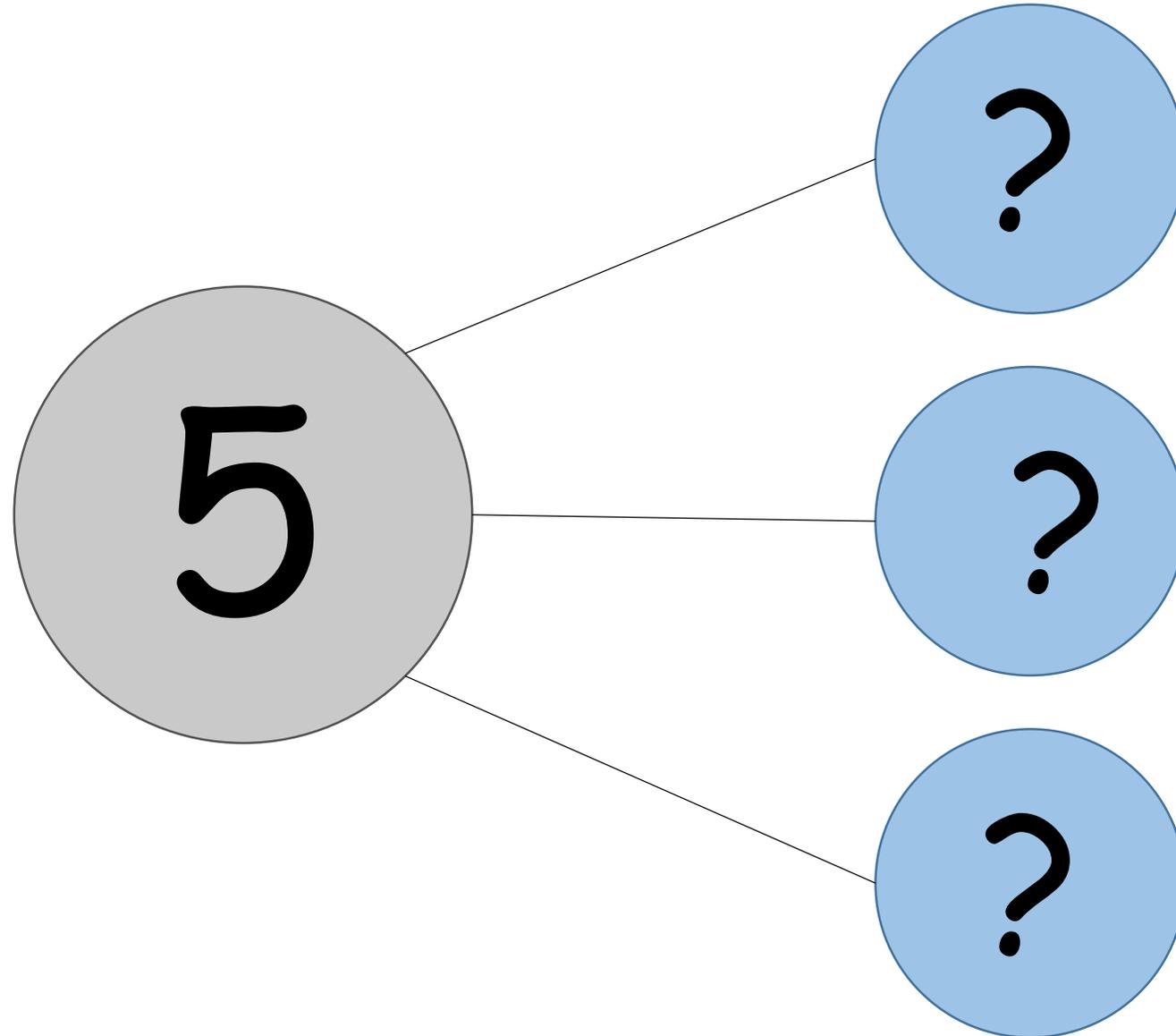




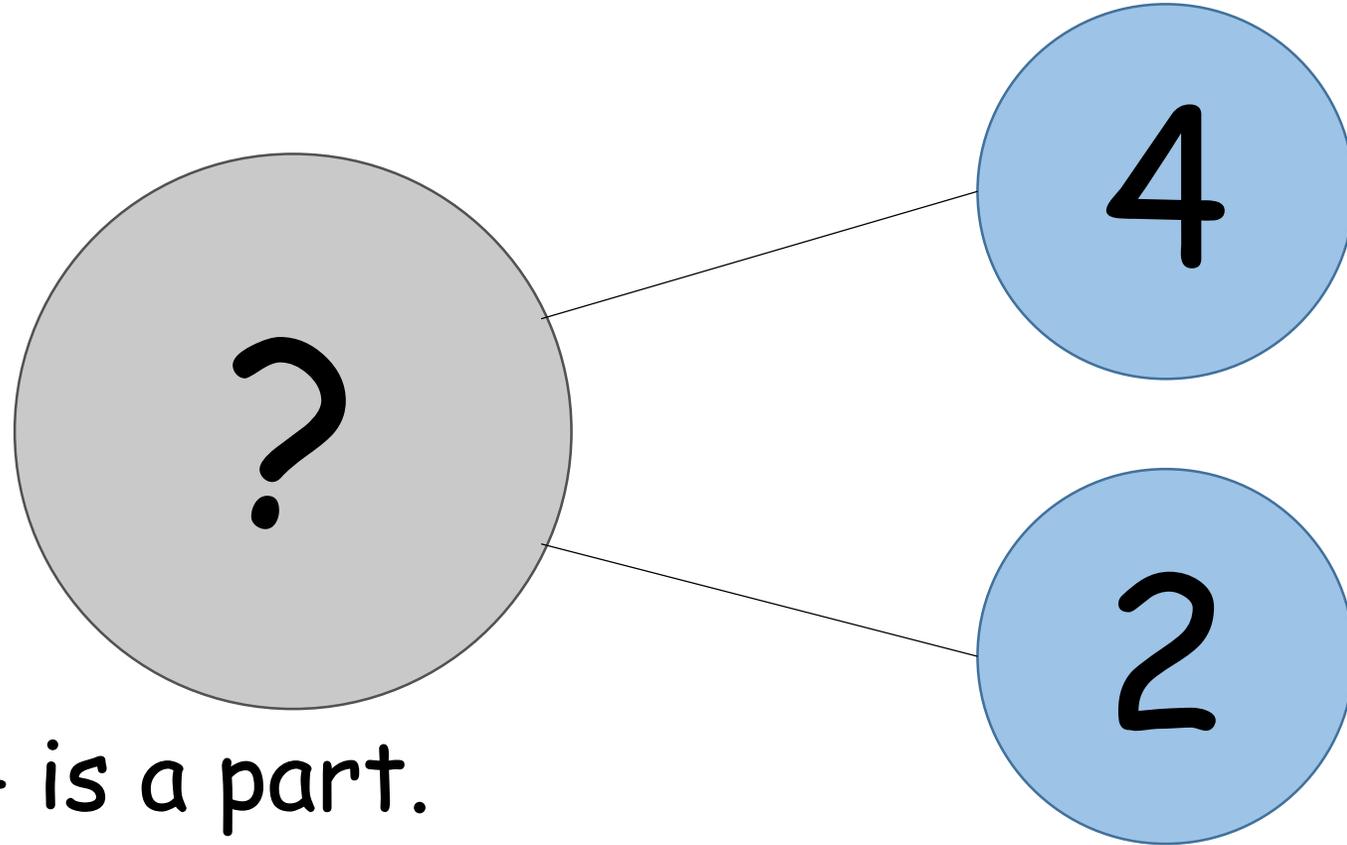
# Variation



# Variation



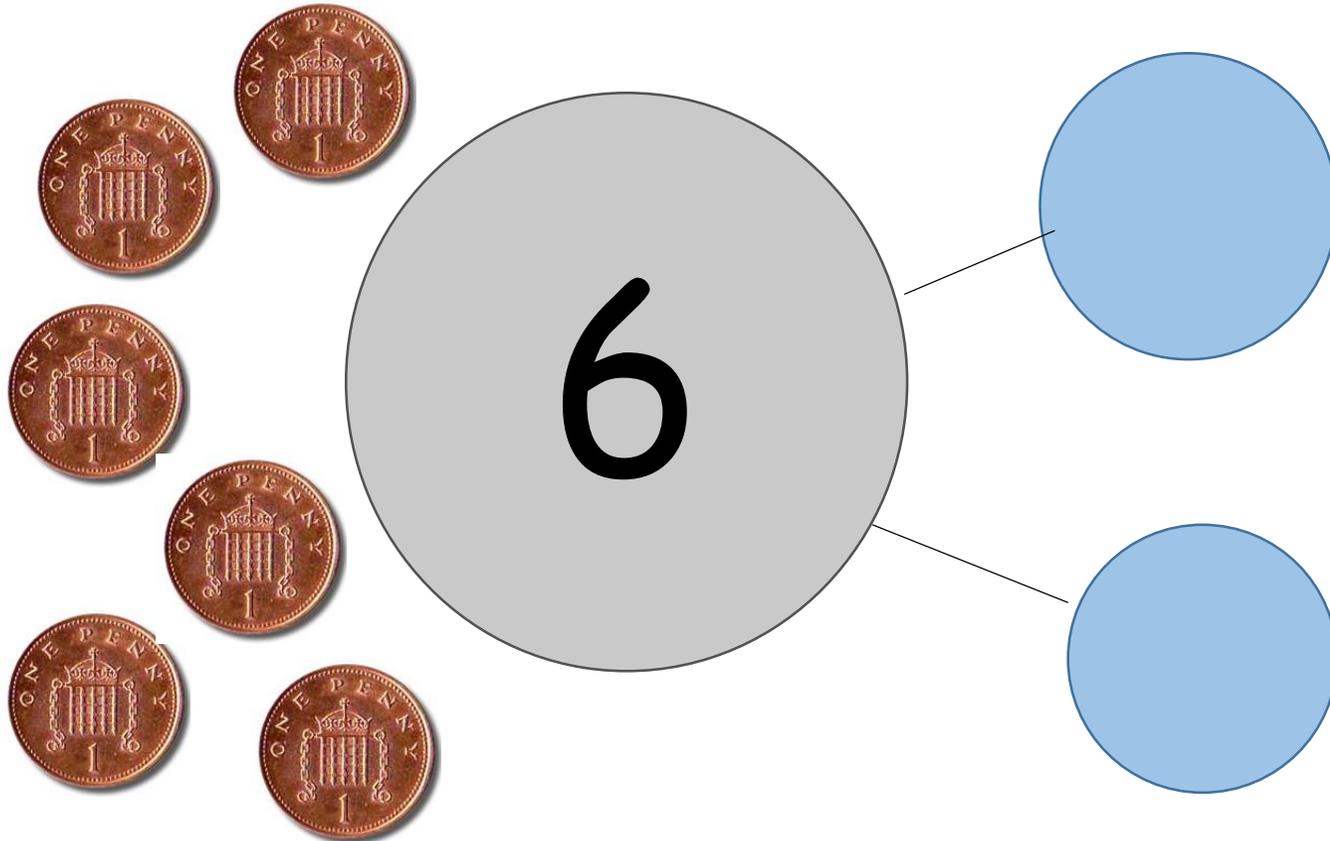
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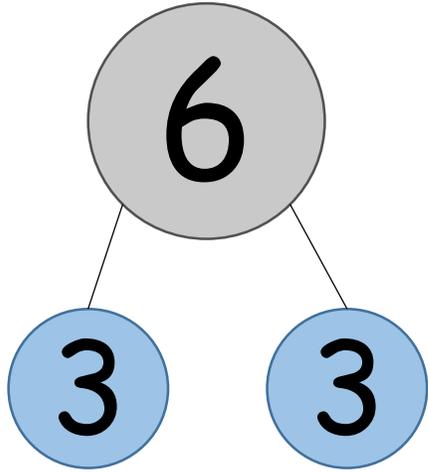


4 is a part.  
2 is a part.  
6 is the whole

## Apply to other maths 'stories' / contexts

Dan's trousers have two pockets and he has 6 pennies in his trouser pockets. How many coins might there be in each pocket?



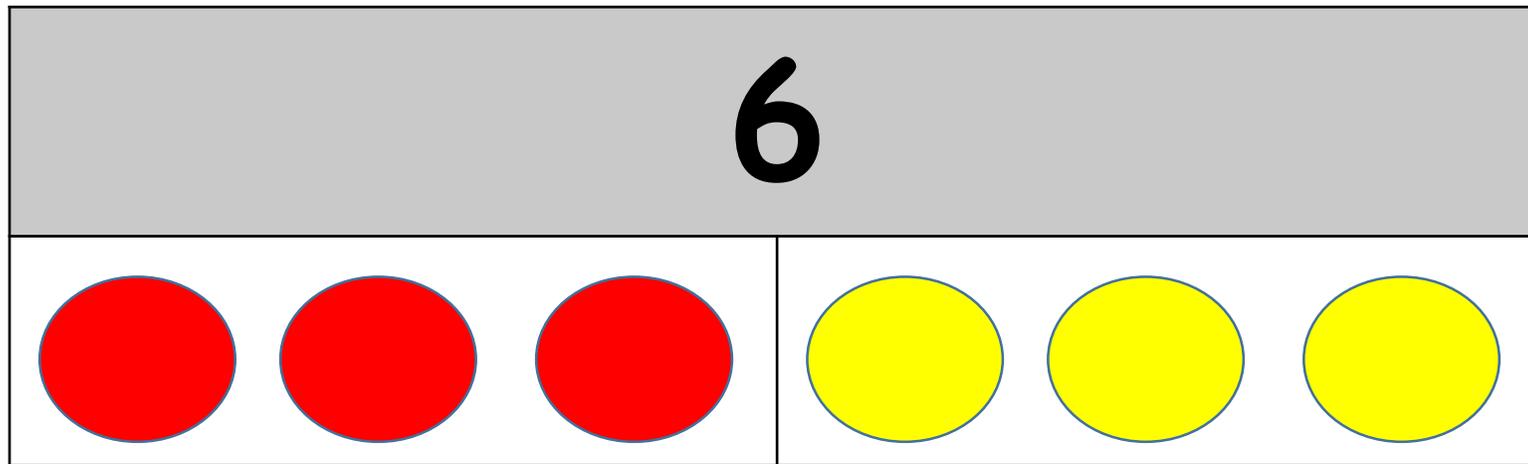


Use of stem sentences.

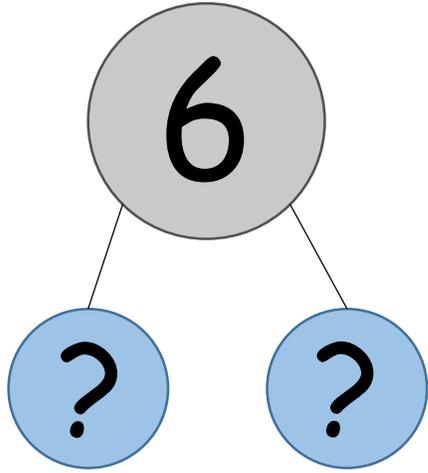
3 is a part.

3 is a part.

6 is the whole

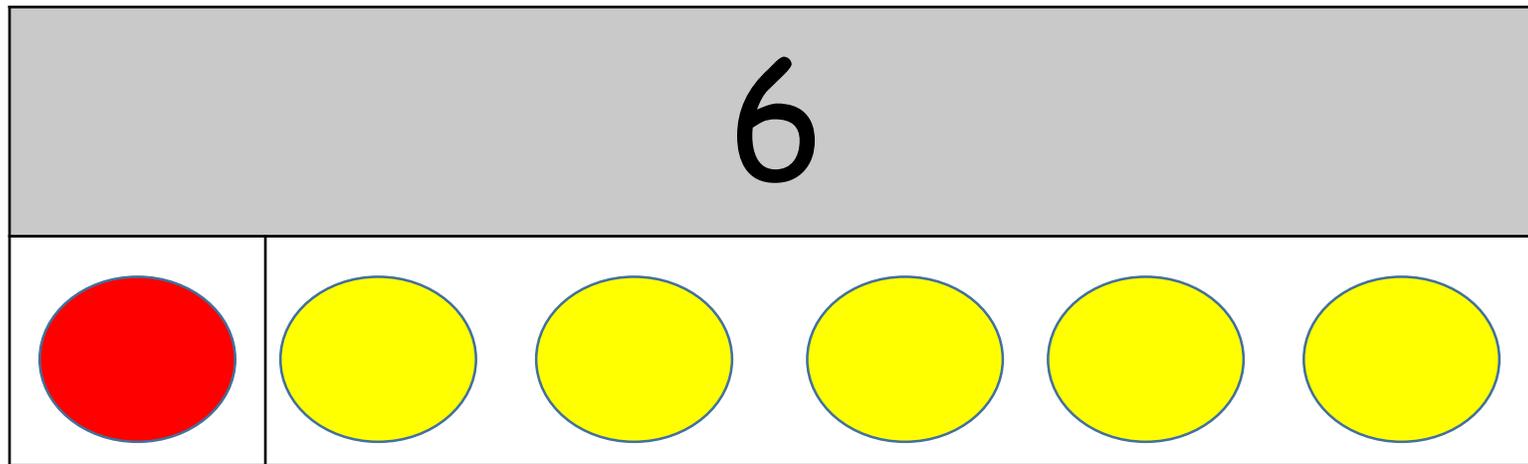


Introducing the bar model

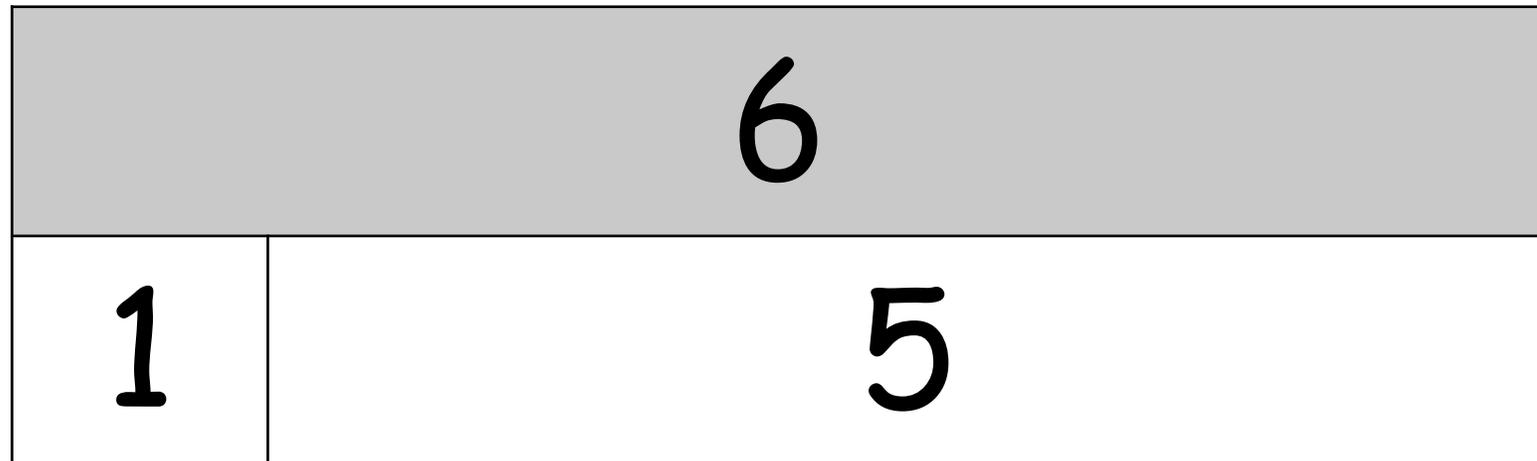
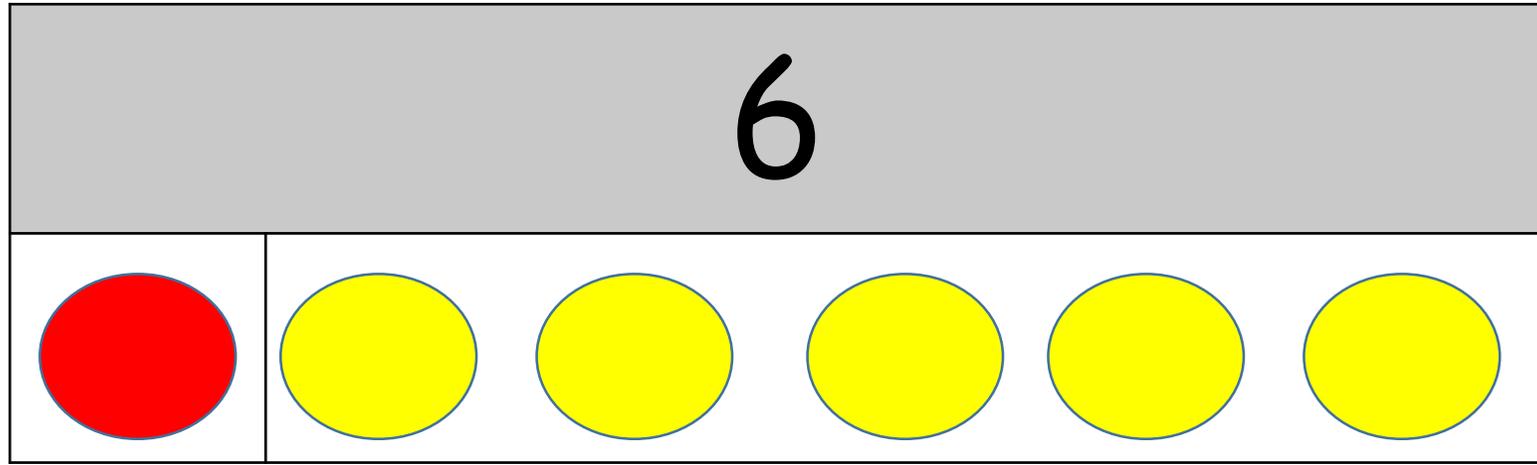


Use of stem  
sentences.

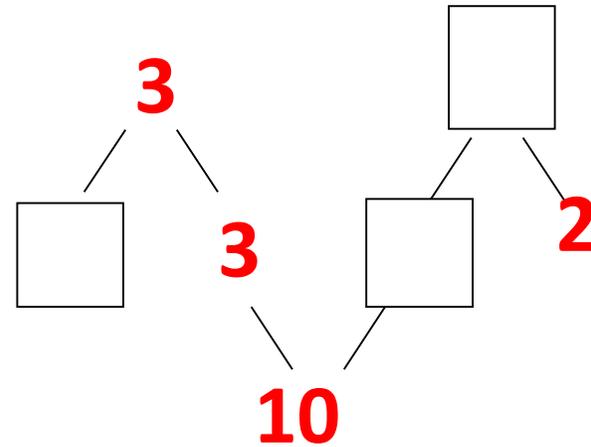
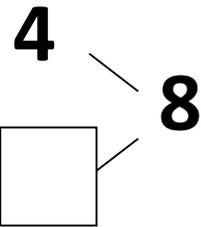
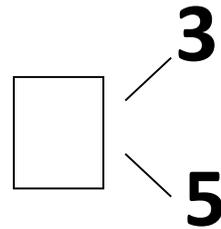
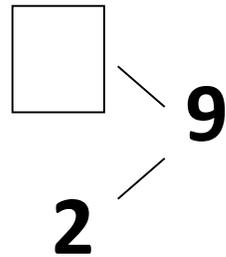
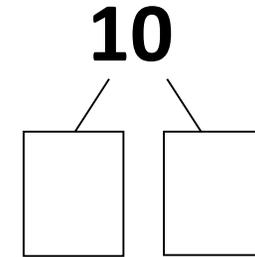
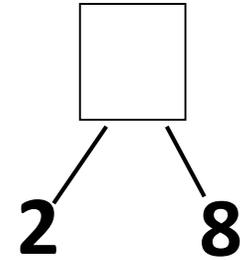
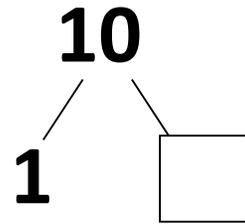
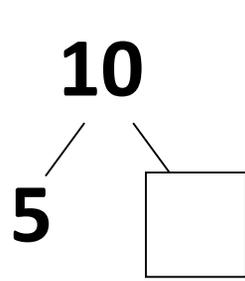
6 is the whole  
1 is a part.  
5 is a part.



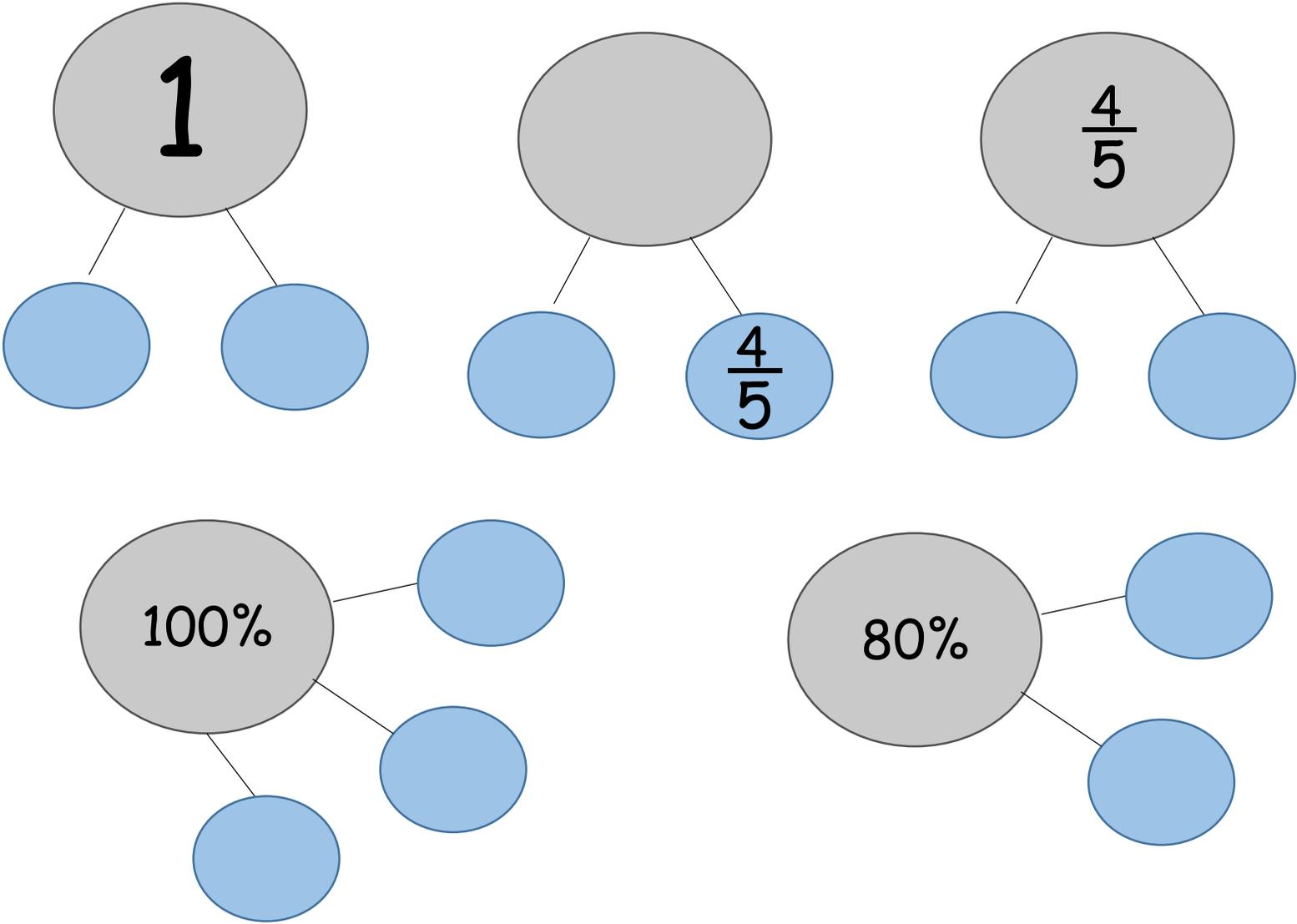
Move from pictorial/ symbolic to abstract.



# Mastery of the part whole model!



How might we use these models with older children?



## Reason



Cory

If the answer to a fraction multiplication is  $\frac{6}{15}$ , one of the fractions which was multiplied could have been  $\frac{2}{3}$ . The answer has not been simplified.

# Proof Explaining Representations

Reason:

$$\frac{2}{3} \times \frac{3}{5} = \frac{6}{15}$$

Yes, Cory is correct because the fraction, when multiplied with  $\frac{3}{5}$  results in the answer  $\frac{6}{15} = \frac{2}{5}$ . Here is a graph to show this:



$\frac{2}{3}$  of  $\frac{3}{5}$

= remaining  $\frac{1}{5}$

Love this explanation!!

(simplified version)

Challenge

$$\frac{6}{8} = \frac{3}{4}$$

(Vf)

If  $3 \times \frac{3}{4} = 2\frac{1}{4}$ , does  $6 \times \frac{6}{8} = 4\frac{2}{8}$ ?

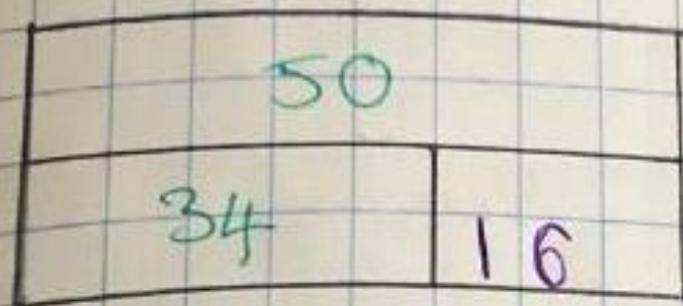
Explain your answer.

$$\frac{6}{1} \times \frac{6}{8} = \frac{36}{8} = 4\frac{4}{8} = \cancel{4\frac{1}{2}}$$

You cannot double a calculation you must re develop the number sentence

# Maths Stories

Q Write a realistic word problem which will use this bar model to solve:



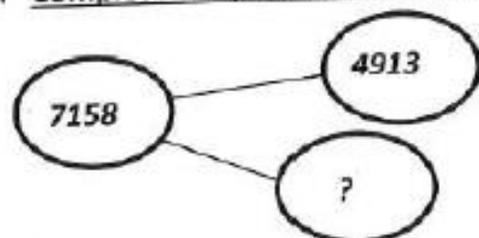
A There are 50 new books delivered to a book shop. 34 of them are hard back. How many are paperback?



A. True or false?

The difference between 8214 and 3192 is 5022.

B. Complete the part-whole model.



C. 9,714 people are at the airport.  
4,532 are men. 4,471 are women.

9714		
4532	4471	?

How many are children? Prove it.

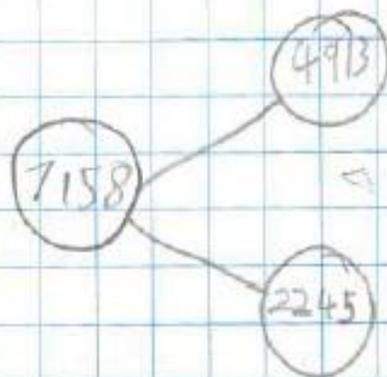
A

$$\begin{array}{r} 8214 \\ - 3192 \\ \hline 5022 \end{array}$$

True ✓

B

$$\begin{array}{r} 7158 \\ - 4913 \\ \hline 2245 \end{array}$$



# True or False

# Different Representations

# Supporting all learners

- Same input for all children
- Ping pong style teaching – all children get a chance to respond
- Group work and talk tasks
- Scaffolds – word bank, extra concrete resources, TA in small group
- Carefully planned questions to address misconceptions
- Carefully planned questions to challenge quick graspers

# Supporting all learners

- Children work on the same independent questions which will be a mix of fluency, problem solving and reasoning.
- The tasks typically get more challenging as the children move through them.
- Children who are struggling may be in a small group to work on one or two tasks with a TA or teacher.
- Children who are comfortable with the learning will be able to choose a “Greater Depth” challenge which will challenge them further while still focusing on the same learning objective.

## In maths lessons ...

- Children are frequently asked to prove their answers.
- We never just tell the children to use a method without explaining why.
- Children are often led to come up with the method by themselves.
- Concrete and pictorial resources are used to help support their understanding.
- Teachers are always asking “Why?”, “How do you know?” and “Are you sure?!”

# Maths at home

The School Run – Maths

<https://www.theschoolrun.com/maths>

Maths Bot – interactive resources and manipulatives

<https://mathsbot.com/>

TT Rockstars – times tables (all children have log ins)

<https://trockstars.com/>

Mathletics – all children have log ins

<https://login.mathletics.com/>

# Questions

